# Extensive and Intensive Margins of Labour Supply: Working Hours in the US, UK and France 

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IFS
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- Preference for leisure? (Blanchard 2004)
- Regulations? (Alesina, Glaeser and Sacerdote 2005)
- Micro vs macro elasticities
- Large vs small variations (Chetty 2009)
- Short-term vs long-term elasticities
- Extensive vs intensive elasticity (Rogerson and Wallenius 2009)


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- Microeconometric studies
- Women with children: Gronau (1974), Heckman (1974,1979), Cogan(1981), Blundell and MaCurdy (1999)
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(1) develop consistent micro-data for an aggregation analysis of three key countries - the US, the UK and France - over the past 30 years
(2) provide a detailed decomposition of the evolution of total hours of work into changes at the extensive and intensive margin
(3) provide a first attempt at consistently estimating micro and macro elasticities on UK data


## - Labour Force surveys

- UK: Labour Force Survey 1975-2008; EFS/FES 1968-2008
- FR: Enquête Emploi 1968-2008
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- Our estimation
- Extensive: employment rate from the reference week
- Intensive: actual hours from the reference week in continuous surveys; usual hours adjusted for annual surveys for France; actual hours adjusted for UK and US for annual surveys


## Total hours

Figure 1: Mean annual hours per individual aged 16 to 74


## Extensive margin

Figure 2: Employment rate (per population) aged 16 to 74


## Intensive margin

Figure 3: Mean annual hours per worker aged 16 to 74


## Total hours by age

Figure 4: Male total hours by age 1977


## Total hours by age

Figure 5: Male total hours by age 2007


## Employment by age

Institute for
Fiscal Studies

Figure 6: Male employment by age 1977


## Employment by age

Institute for Fiscal Studies

Figure 7: Male employment by age 2007


## Total hours by age

Figure 8: Female total hours by age 1977


## Total hours by age

Figure 9: Female total hours by age 2007


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Figure 10: Female employment by age 1977


## Employment by age

Figure 11: Female employment by age 2007


## Variations within the year

Table 1: Weekly hours and weeks worked (2007)

|  | Men |  |  | Women |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FR | UK | US | FR | UK | US |
| Annual hours (all) | 1800 | 1919 | 2107 | 1445 | 1389 | 1792 |
| Share part-time | $5.0 \%$ | $10.5 \%$ | $10.1 \%$ | $29.4 \%$ | $41.9 \%$ | $23.9 \%$ |
|  |  |  |  |  |  |  |
| Full-time workers |  |  |  |  |  |  |
| Annual hours | 1839 | 2044 | 2229 | 1631 | 1777 | 2041 |
| Weekly hours | 42.1 | 46.8 | 44.6 | 39.0 | 43.5 | 42.0 |
| Weeks worked | 43.7 | 43.7 | 50.0 | 41.8 | 40.9 | 48.5 |
|  |  |  |  |  |  |  |
| Part-time workers |  |  |  |  |  |  |
| Annual hours | 995 | 857 | 1030 | 1008 | 851 | 1021 |
| Weekly hours | 22.5 | 22.2 | 21.3 | 23.7 | 22.9 | 21.5 |
| Weeks worked | 44.2 | 38.6 | 48.4 | 42.5 | 37.1 | 47.5 |

## Variations within the year

Figure 12: Actual weekly hours by month of the year (2002-2008)


## Decomposing Changes in Hours

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- where each $H_{j t}$ can be expressed as the product of hours per worker $h_{j t}$ and participation in the labour market $p_{j t}$

$$
H_{j t}=p_{j t} h_{j t} .
$$

## Decomposing Changes in Hours

- We measure the change due to the behavior of category $j$, holding the population structure constant as in date $t-1$, as in a Laspeyres index

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\Delta_{j t}=q_{j, t-1}\left[H_{j t}-H_{j, t-1}\right] .
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$$

- where $S_{t}$ measures the change in the composition of the population:

$$
S_{t}=\sum_{j=1}^{J} H_{j t}\left[q_{j t}-q_{j, t-1}\right] .
$$

Table 2: Decomposing the change in total hours, 1977-2007

|  | Year | Youth (16-29) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Wemen | Prime aged (30-54) |  | Old (55-74) |  |  |  |  |
| Wen | Women | Men | Women |  |  |  |  |
| FR | 1977 | 1402 | 871 | 2010 | 951 | 827 | 367 |
|  | 2007 | 858 | 627 | 1639 | 1116 | 508 | 344 |
|  | $\Delta_{j}$ | -82 | -38 | -82 | 36 | -36 | -3 |
| UK | 1977 | 1707 | 938 | 2117 | 873 | 1107 | 323 |
|  | 2007 | 1219 | 876 | 1786 | 1055 | 790 | 385 |
|  | $\Delta_{j}$ | -71 | -9 | -70 | 39 | -42 | 10 |
| US | 1977 | 1344 | 835 | 2018 | 947 | 1025 | 447 |
|  | 2007 | 1236 | 956 | 1922 | 1373 | 1084 | 754 |
|  | $\Delta_{j}$ | -19 | 22 | -19 | 90 | 6 | 38 |

Sources: Enquête Emploi, Labour Force Survey, Current Population Survey.

- evolution of total $\Delta$ differs: - 195 for FR, -118 for UK, +165 for US.

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- evolution of total $\Delta$ differs: - 195 for FR, -118 for UK, +165 for US.
- composition S: +10 for FR, +25 for UK, +46 for US

Figure 13: Decomposing the change in total hours (1977-2007)


## Intensive vs extensive margins

- We decompose the change in total hours for the $j$ type $\Delta_{j}$ into:
- an intensive component $l_{j}=p_{l j} \Delta h_{j}$
- an extensive component $E_{j}=h_{E j} \Delta p_{j}$

$$
\Delta_{j t}=I_{j}+E_{j}
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- We get intensive bounds
- Assuming $p_{l j} \in\left[p_{j, t-1}, p_{j t}\right]$

$$
\begin{gathered}
I_{j} \in\left[p_{j, t-1}\left(h_{j t}-h_{j, t-1}\right), p_{j, t}\left(h_{j t}-h_{j, t-1}\right)\right] \\
I_{j} \in[I-\text { Laspeyres, } I-\text { Paasche }]
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- We get extensive bounds
- From the identity $\Delta_{j t}=I_{j}+E_{j}$

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## Bounding Changes

- At the limits, the change in total hours for any type $j$ satisfies two polar exact statistical decompositions:

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\begin{align*}
\Delta_{j t} & =q_{j, t-1}\left\{\left[h_{j t}-h_{j t-1}\right] p_{j t}+\left[p_{j t}-p_{j t-1}\right] h_{j t-1}\right\}  \tag{1}\\
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or

$$
\begin{gather*}
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\Delta_{j t}=q_{j, t-1}\{I-\text { Laspeyres }+E-\text { Paasche }\}
\end{gather*}
$$

## Bounding changes

Figure 14: Decomposing the changes at the extensive and intensive margins by age and gender (1977-2007)

|  | Year | Men <br> $16-29$ | Women <br> $16-29$ | Men <br> $30-54$ | Women <br> $30-54$ | Men <br> $55-74$ | Women <br> $55-74$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FR | I-P, I-L | $[-37,-28]$ | $[-23,-19]$ | $[-59,-56]$ | $[-49,-35]$ | $[-11,-8]$ | $[-10,-9]$ |
|  | E-L, E-P | $[-54,-45]$ | $[-19,-16]$ | $[-27,-23]$ | $[71,85]$ | $[-28,-25]$ | $[6,7]$ |

## The young

Figure 15: Share of the 16-29 population in work


## The young

Figure 16: Share of the 16-29 population looking for work


## The young

Figure 17: Share of the 16-29 population in school and not in work


## Older workers

Figure 18: Male employment rate from 50 to 74 (1977)


## Older workers

Figure 19: Male employment rate from 50 to 74 (2007)


## Recovering elasticities

## - Objectives

- Link up these changes at the extensive and intensive margins to movements in the distribution of taxes, relative wages, demographics and other incomes.
- Draw implication for extensive and intensive elasticities
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- Aggregation issues
- How is the aggregate labour supply elasticity related to various micro elasticities?
- Empirical issues (forthcoming)
- Use IFS microsimulation model TAXBEN
- Estimation extensive and intensive elasticities
- Similar approach for France and the US


## Aggregation

- Consider preferences

$$
U= \begin{cases}\lambda R(h)+\frac{(T-h)^{1-1 / \alpha}}{1-1 / \alpha}-\beta & \text { if } h>0 \\ \lambda s & \text { if } h=0\end{cases}
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- The 'aggregate' hours elasticity is given by
$\varepsilon=\frac{1}{\tilde{H}} \int_{w} \int_{\alpha} \int_{\lambda} p() h()\left[\varepsilon_{l}(\alpha, \lambda, w)+\varepsilon_{E}(\alpha, \lambda, w)\right] g(\alpha, \lambda, w) d \alpha d \lambda d w$.


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- $h(\alpha, \lambda, w)$ hours, $p(\alpha, \lambda, w)$ proportion of type $(\alpha, \lambda, w)$ workers


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- We have shown that the aggregate evolution cannot be ascribed to a single cause but covers very diverse movements at the extensive and extensive margins by age and gender.


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- We have shown that the aggregate evolution cannot be ascribed to a single cause but covers very diverse movements at the extensive and extensive margins by age and gender.
- We have developed an approach to estimating the total hours elasticity from the distribution of micro elasticities at the extensive and intensive margins.

