Intergenerational Mobility in Socio-emotional Skills

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Motivation and Research Question

Motivation:

- Different types of skills are important determinants of many life outcomes. (e.g., Almlund et al. (2011))
- Parental skill endowments and investment play an important role in determining their children's skills. (e.g., Cunha and Heckman (2007))

Research question:

- Are **parental skills** *during childhood* transmitted to their children *during childhood*?
- Are grandmothers' skills transmitted too?

Preview of the Findings

In the United Kingdom:

- Parental skills at ages 5, 10 and 16 predict their children's socio-emotional skills during childhood
- Persistence increases if we measure parental skills at later ages
- **Stronger** transmission from **mothers to children**
- Sevidence on multigenerational mobility in socio-emotional skills.

Overview

Data

Literature

Measuring Mobility in Skills

Mobility Estimates

Multi-generational Mobility

Conclusion

Data: 1970 British Cohort Study

- Longitudinal database following the lives of people born in a single week of 1970 in England, Scotland and Wales.
- Cohort members have been interviewed ten times since 1970.
 - Parents' socio-emotional skills during childhood (Age-5, 10, and 16 waves).
 - Parents' socio-emotional skills during adulthood (Age-26 ad 34 waves).
- Link parents to their children (aged 3-16) from the age-34 wave.

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Literature on intergenerational and multigenerational mobility in skills.

Anger (2012), Dohmen et al. (2011), Gronqvist et al. (2016), Alana et al. (2017), Loehlin (2005), Johnson et al. (2013) and many others...

This paper:

- We use multiple measures of socio-emotional skills collected in different waves during childhood and during adulthood.
- Parents' and children's skills are <u>not</u> contemporaneously measured.

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Modelling the Dimensions of Socio-emotional Skills

- Focus on two dimensions of socio-emotional skills EFA
 - internalising: ability to focus attention
 - externalising: ability to engage in interpersonal activities
- Use questionnaire items from Rutter A (parents) and Strengths and Difficulties (children) Questionnaires. Rutter SDQ

Dimensions of Socio-emotional Skills

Factor	Cat.	Title	Rutter Wording (Parents during childhood)	SDQ Wording (Children aged 3-16)
EXT	3	Restless	Very restless. Often running about or	Restless, overactive and
			jumping up and down. Hardly ever still	not able to sit still for long
EXT	3	Squirmy/fidgety	Is squirmy or fidgety.	Constantly fidgeting and squirming
EXT	3	Fights/bullies	Frequently fights other children	Has often had fights
				with other children or bullied them
EXT	3	Distracted	Cannot settle to anything	Easily distracted, concentration wandered
			for more than a few moments.	
EXT	2/3	Tantrums	Has temper tantrums (that is, complete loss of temper	Has often had temper tantrums or
	,		with shouting, angry movements, etc.)	hot tempers
EXT	3	Disobedient	Is often disobedient	(+) Generally obedient, usually doing what
				adults requested
INT	3	Worried	Often worried, worries about many things	Many worries, often seeming worried
INT	3	Fearful	Tends to be fearful or afraid	Nervous or clingy in new situations,
			of new things or new situations	easily loses confidence
INT	3	Solitary	Tends to do things on his/her own,	Rather solitary,
			is rather solitary	tending to play alone
INT	3	Unhappy	Often appears miserable, unhappy, tearful or	Often unhappy, downhearted or tearful
	-		distressed	
INT	2/3	Aches	Complains of headaches +	Often complaining of headaches, stomach-aches
	, -		stomach-ache or has vomited	or sickness

Modelling the Dimensions of Socio-emotional Skills

- Focus on two dimensions of socio-emotional skills
 - internalising: ability to focus attention
 - externalising: ability to engage in interpersonal activities
- Use questionnaire items, Z_{ijc}, from Rutter A (parents) and Strengths and Difficulties (children) Questionnaires. Rutter SDQ
- Multigroup factor model with categorical items Model

$$Z^*_{ijc} = v_{jc} + \lambda_{jc}^\top Y_{ic} + u_{ijc}.$$

$$Z_{ijc} = \begin{cases} 0 & \text{if } Z_{ijc}^* < \tau_{1,jc} \\ 1 & \text{if } Z_{ijc}^* \in [\tau_{1,jc}, \tau_{2,jc}] \\ 2 & \text{if } Z_{ijc}^* > \tau_{2,jc} \end{cases}$$

Exploratory Factor Analysis: Factor Loadings

	Parents (age 5)		Parents	Parents (age 10)		Parents (age 16)		Children	
Item	EXT	INT	EXT	INT	EXT	INT	EXT	INT	
Restless	0.8648	-0.1281	0.8108	-0.1640	0.8000	-0.1228	0.6040	0.0785	
Squirmy/fidgety	0.7816	0.0100	0.6919	0.0263	0.7286	0.0103	0.6166	0.1066	
Fights/bullies	0.4830	0.2039	0.4955	0.0021	0.6111	0.0058	0.6875	-0.005	
Distracted	0.6431	0.0556	0.5927	0.0705	0.6493	0.0709	0.7113	0.0553	
Tantrums	0.5466	0.1570	0.4892	0.1756	0.4998	0.1262	0.7244	-0.016	
Disobedient	0.5732	-0.0575	0.6684	0.0288	0.6890	-0.0016	0.8162	-0.178	
Worried	-0.1092	0.7993	-0.0981	0.7030	-0.0055	0.7953	-0.0701	0.7747	
Fearful	0.0657	0.4692	-0.0921	0.5659	-0.1245	0.7277	-0.0798	0.6837	
Solitary	-0.0391	0.4794	0.0989	0.2828	0.0463	0.3125	0.1060	0.4432	
Unhappy	0.0492	0.7948	0.2346	0.5117	0.2664	0.5016	0.3889	0.4102	
Aches	-0.0078	0.5367	-0.0492	0.4103	-0.0360	0.3897	0.1322	0.175	

Note. The table displays the factors loadings obtained from exploratory factor analysis (EFA) by sample. The EFA is based on the decomposition of the polychoric correlation matrix, and uses oblimin rotation. Since they are all behaviours indicating lower skills, we recode all of them in reverse, i.e. 'Certainly applies' = 0, 'Somewhat applies' = 1, 'Does not apply' = 2.

Modelling the Dimensions of Socio-emotional Skills

- Focus on two dimensions of socio-emotional skills
 - internalising: ability to focus attention
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$$Z_{ijc}^* = v_{jc} + \lambda_{jc}^\top Y_{ic} + u_{ijc}.$$

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Test for measurement invariance Measurement invariance

Relative Mobility in Socio-emotional Skills

$$Y_i^{C} = \alpha + \beta^{\top} \mathbf{Y}_i^{P} + \rho^{\top} \mathbf{X}_i + \epsilon_i$$
(1)

- Y_i^C : **Child**'s socio-emotional skills during childhood
- **Y**^{*P*}_{*i*}: **parent**'s skills (internalising, externalising and cognitive) during childhood
- X_i: Vector of **controls**, which include the region of birth fixed effects, the parent's gender, the child's gender and age, the number of children in the household, the mother's age at the parent's birth, a dummy equal to 1 if the parent is the first born, the parent's employment status at the age of 34, the grandparent's employment status and education in 1975 and the number of children in the parent's household when the parent is 5 years old.
- ϵ_{it} : error term
- Higher values of the coefficient β correspond to lower mobility.

Absolute Mobility in Socio-emotional Skills

Estimate the children's outcomes (R_i^C) from parents (R_i^P) at a given quintile in the distribution. For example,

$$LH = Pr(R_i^C \ge 80|R_i^P < 20).$$
⁽²⁾

Produce matrices of transition probabilities across quintile of skill distribution.

To facilitate comparisons across the several matrices, we propose:

- 'spectral gap mobility index': (1 second largest eigenvalue)
- How far the intergenerational transition matrices are from an identity matrix, which corresponds to no mobility.

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Relative Mobility in Socio-emotional Skills

Dependent variable:	Child's					
	Internalisir	Externalis	ing (EXT)			
	(1)	(2)	(3)	(4)		
Parent's INT (during childhood)	0.168***	0.192***				
· - /	(0.050)	(0.067)				
Parent's EXT (during childhood)	(<i>)</i>	-0.082				
(, ,		(0.071)				
Parent's COG (during childhood)		0.157**				
		(0.052)				
Observations	1035	1035				
R^2	0.027	0.135				
Region of birth FE (BCS70 5y)	No	Yes				
Child's age FE	No	Yes				
Other controls	No	Yes				

Note. The measurement system and the intergenerational mobility equation are estimated jointly. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

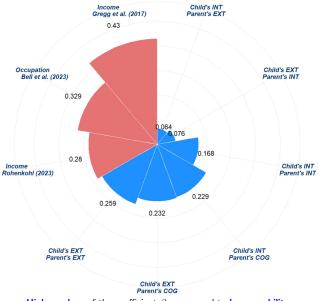
Relative Mobility in Socio-emotional Skills

Dependent variable:	Child's					
	Internalisir	ng (INT)	Externalisir	ng (EXT)		
	(1)	(2)	(3)	(4)		
Parent's INT (during childhood)	0.168***	0.192***		-0.040		
· - /	(0.050)	(0.067)		(0.057)		
Parent's EXT (during childhood)	()	-0.082	0.259***	0.243 ^{***}		
· - /		(0.071)	(0.047)	(0.054)		
Parent's COG (during childhood)		0.157 ^{**}	、	0.153 ^{***}		
		(0.052)		(0.041)		
Observations	1035	1035	1035	1035		
R^2	0.027	0.135	0.063	0.165		
Region of birth FE (BCS70 5y)	No	Yes	No	Yes		
Child's age FE	No	Yes	No	Yes		
Other controls	No	Yes	No	Yes		

Note. The measurement system and the intergenerational mobility equation are estimated jointly. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

Teachers' measures

Comparison of Mobility Measures in the UK



Higher values of the coefficient β correspond to lower mobility.

Mobility in Skills with Contemporaneous Measures

Dependent variable:	Internalising (INT) Skill				
	Child	Child	Child		
	(1)	(2)	(3)		
Parent's INT (during childhood)	0.208***		0.137*		
	(0.067)		(0.078)		
Parent's INT (contemporaneous - age 34)		0.426***	0.393***		
		(0.077)	(0.090)		
Observations	919	919	919		
R^2	0.093	0.198	0.208		
Region of birth FE (BCS70 5y)	Yes	Yes	Yes		
Child's age FE	Yes	Yes	Yes		
Other controls	Yes	Yes	Yes		

Note. The measurement system and the intergenerational mobility equation are estimated jointly. The internalising skill is derived by a factor model that considers 3 items (unhappy, worried and fearful) common across the 4 different sweeps. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p<0.01, ** p<0.05, * p<0.1).

Scatter plots

Mobility in Socio-emotional Skills by Gender

Panel A: Mother-child				
Dependent variable:	Child's Internalis	Child's Externalising (EXT) Skill		
	(1)	(2)	(3)	(4)
Parent's INT (during childhood)	0.219***	0.221***		-0.065
()	(0.062)	(0.081)		(0.074)
Parent's EXT (during childhood)		-0.096	0.300***	0.288***
· - ,		(0.079)	(0.054)	(0.072)
Parent's COG (during childhood)		0.173**		0.190***
		(0.063)		(0.058)
Observations	752	752	752	752
R ²	0.046	0.159	0.083	0.182
Region of birth FE (BCS70 5y)	No	Yes	No	Yes
Child's age FE	No	Yes	No	Yes
Other controls	No	Yes	No	Yes
Panel B: Father-child				
Dependent variable:	Child's Internalising (INT) Skill		Child's Externalising (EXT) Skill	
	(1)	(2)	(3)	(4)
Parent's INT (during childhood)	-0.011	0.152		0.070
	(0.109)	(0.158)		(0.171)
Parent's EXT (during childhood)		-0.099	0.094	0.045
		(0.150)	(0.104)	(0.159)
Parent's COG (during childhood)		0.164		0.114
		(0.145)		(0.114)
Observations	283	283	283	283
R ²	0.000	0.165	0.009	0.174
Region of birth FE (BCS70 5y)	No	Yes	No	Yes
Child's age FE	No	Yes	No	Yes
Other controls	No	Yes	No	Yes

Note. The measurement system and the intergenerational mobility equation are estimated jointly. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

Mobility in Socio-emotional Skills by Gender

Panel A: Parent-child same gender				
Dependent variable:	Child's Internalis	Child's Externalising (EXT) Skill		
	(1)	(2)	(3)	(4)
Parent's INT (during childhood)	0.233***	0.271***		-0.032
(, ,	(0.069)	(0.091)		(0.073)
Parent's EXT (during childhood)		-0.106	0.241***	0.187***
· · · · ·		(0.096)	(0.059)	(0.077)
Parent's COG (during childhood)		0.073	. ,	0.163***
		(0.089)		(0.065)
Observations	539	539	539	539
R ²	0.051	0.218	0.167	0.189
Region of birth FE (BCS70 5y)	No	Yes	No	Yes
Child's age FE	No	Yes	No	Yes
Other controls	No	Yes	No	Yes
Panel B: Parent-child different gender				
Dependent variable:	Child's Internalising (INT) Skill		Child's Externalising (EXT) Skill	
	(1)	(2)	(3)	(4)
Parent's INT (during childhood)	0.078	0.072		-0.055
	(0.088)	(0.114)		(0.095)
Parent's EXT (during childhood)		-0.036	0.280***	0.300***
		(0.140)	(0.063)	(0.096)
Parent's COG (during childhood)		0.253***		0.140*
		(0.114)		(0.077)
Observations	496	496	496	496
R ²	0.006	0.083	0.073	0.148
Region of birth FE (BCS70 5y)	No	Yes	No	Yes
Child's age FE	No	Yes	No	Yes
Other controls	No	Yes	No	Yes

Note. The measurement system and the intergenerational mobility equation are estimated jointly. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

Absolute Mobility in Socio-emotional Skills

Child's $E \wedge I = Parent's E \wedge I (during childhood)$									
	Parent quintile								
		1	2	3	4	5			
	1	33.5	15.9	19.3	14.9	12.5			
	2	21.3	21.7	21.7	17.8	19.9			
Child quintile	3	18.3	21.3	22.2	18.3	19			
	4	12.7	21.3	13.5	24.0	26.9			
	5	14.2	19.8	23.2	25.0	21.8			
Spectra	ոլ ռու	n mohilit	v indev	0.800 ((0.038)				

Child's EXT Parent's EXT (during childhood)

Spectral gap mobility index: 0.800 (0.038)

		Parent quintile							
		1 2 3 4 5							
	1	22.7	20.4	18.8	16.9	16.6			
	2	21.2	25.7	17.4	19.8	17.1			
Child quintile	3	22.2	18.4	24.2	18.8	16.6			
	4	18.7	18.4	20.3	21.7	23			
	5	15.2	17	19.3	22.7	26.7			

Child's INT - Parent's INT (during childhood)

Spectral gap mobility index: 0.885 (0.034)

Note. All standard errors of the spectral gap mobility index in parentheses are obtained using 200 bootstrap repetition, taking into account the factor estimation stage that precedes the estimation of the transition matrix and its respective eigenvalues.

Correlation between relative mobility and spectral gap mobility index = -0.898

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Multigenerational Mobility in Socio-emotional Skills

- **Grandmothers** (aged around 25 years old) completed the Mother Malaise Questionnaire at age-5, 10 and 16 waves.
- Use **comparable** questionnaires items across 3 generation to derive:

 \Rightarrow **Internalising skill** from items: (i) worried, (ii) fearful, (iii) unhappy, (iv) aches, and (v) solitary.

Multigenerational Mobility in Socio-emotional Skills

Dependent variable:	Grandchild's I	nternalising	Grandchild's Externalising		
	(1)	(2)	(3)	(4)	
Grandmother's INT	0.138***	0.074			
	(0.053)	(0.075)			
Parent's COG (during childhood)	()	0.184 ^{***}			
(, ,		(0.049)			
Parent's EXT (during childhood)		-0.094			
		(0.063)			
Parent's INT (during childhood)		0.145 [*]			
, , ,		(0.075)			
Observations	994	994			
R^2	0.078	0.115			
Region of birth FE (BCS70 5y)	Yes	Yes	Yes	Yes	
Child's age FE	Yes	Yes	Yes	Yes	
Other controls	Yes	Yes	Yes	Yes	

Note. The measurement system and the mobility equation are estimated jointly. Other controls include the cohort member's gender, the age of the cohort member's mother at birth, the grandchild's gender. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

Multigenerational Mobility in Socio-emotional Skills

Dependent variable:	Grandchild's	nternalising	Grandchild's Externalising		
	(1)	(2)	(3)	(4)	
Grandmother's INT	0.138***	0.074	0.159***	0.108*	
	(0.053)	(0.075)	(0.043)	(0.057)	
Parent's COG (during childhood)	· · · ·	0.184 ^{***}	· · ·	0.191***	
(C)		(0.049)		(0.044)	
Parent's EXT (during childhood)		-0.094		0.221***	
()		(0.063)		(0.051)	
Parent's INT (during childhood)		0.145 [*]		-0.106*	
(C)		(0.075)		(0.062)	
Observations	994	994	994	994	
R^2	0.078	0.115	0.063	0.141	
Region of birth FE (BCS70 5y)	Yes	Yes	Yes	Yes	
Child's age FE	Yes	Yes	Yes	Yes	
Other controls	Yes	Yes	Yes	Yes	

Note. The measurement system and the mobility equation are estimated jointly. Other controls include the cohort member's gender, the age of the cohort member's mother at birth, the grandchild's gender. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).

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Examine how skills are transmitted across generations during childhood.

- Main findings:
 - Parental skills during childhood predict their child's socio-emotional development during childhood
 - Grandmothers' internalising skill predicts their grandchildren's socio-emotional development.
- Heterogeneity:
 - Skill transmission becomes more persistent as parents age
 - **2** Skill transmission occurs mostly from mothers to children.

Rutter A questionnaire

Rutter A scale administered to parents when they were 5, 10 and 16 years old 1. Very restless. Often running about or jumping up and down. Hardly ever still.* 2. Is squirmy or fidgety.* 4. Frequently fights other children.* 3. Often destroys own or others' belongings. 5. Not much liked by other children. 6. Often worried, worries about many things.* 7. Tends to do things on his/her own, is rather solitary.* 8. Irritable. Is guick to fly off the handle. 9. Often appears miserable, unhappy, tearful or distressed.* 10. Sometimes takes things belonging to others. 11. Has twitches, mannerisms or tics of the face or body. 12. Frequently sucks thumb or finger. 14. Is often disobedient.* 13. Frequently bites nails or fingers. 15. Cannot settle to anything for more than a few moments.* 16. Tends to be fearful or afraid of new things or new situations.* 17. Is over fussy or over particular. 18 Often tells lies 19 Bullies other children * A. Complains of headaches.* B. Complains of stomach-ache or has vomited.* C. Complains of biliousness D. Has temper tantrums (that is, complete loss of temper with shouting, angry movements, etc.).*

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Strengths and Difficulties Questionnaire

Strengths and Difficulties Questionnaire scale administered to children when they were between the age 3-16

- 1. Considerate of other people's feelings+
- 3. Often complaining of headaches, stomach-aches or sickness*
- 5. Has often had temper tantrums or hot tempers*
- 7. Generally obedient, usually doing what adults requested* +
- 9. Helpful if someone was hurt, upset or feeling ill⁺
- 11. Has had at least one good friend +
- 13. Often unhappy, downhearted or tearful*
- 15. Easily distracted, concentration wandered*
- 17. Kind to younger children +
- 19. Picked on or bullied by other children
- 21. Able to think things out before acting † +
- 23. Getting on better with adults than with other children
- 25. Has seen tasks through to the end, good attention span $^+$

- 2. Restless, overactive and not able to sit still for long*
- 4. Sharing readily with other children (treats, toys, pencils etc.)+
- 6. Rather solitary, tending to play alone*
- 8. Many worries, often seeming worried*
- 10. Constantly fidgeting and squirming*
- 12. Has often had fights with other children or bullies them*
- 14. Generally liked by other children +
- 16. Nervous or clingy in new situations, easily loses confidence*
- 18. Often lied or cheated[†]
- 20. Has often volunteered to help others (parents, teachers, other children)+
- 22. Stole from home, school or elsewhere
- 24. Many fears, easily scared

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Exploratory Factor Analysis: Factor Loadings

	Parents (age 5)		Parents (age 10)		Parents (age 16)		Children	
Item	EXT	INT	EXT	` INŤ	EXT	INŤ	EXT	INT
Restless	0.8648	-0.1281	0.8108	-0.1640	0.8000	-0.1228	0.6040	0.0785
Squirmy/fidgety	0.7816	0.0100	0.6919	0.0263	0.7286	0.0103	0.6166	0.1066
Fights/bullies	0.4830	0.2039	0.4955	0.0021	0.6111	0.0058	0.6875	-0.0050
Distracted	0.6431	0.0556	0.5927	0.0705	0.6493	0.0709	0.7113	0.0553
Tantrums	0.5466	0.1570	0.4892	0.1756	0.4998	0.1262	0.7244	-0.0164
Disobedient	0.5732	-0.0575	0.6684	0.0288	0.6890	-0.0016	0.8162	-0.1781
Worried	-0.1092	0.7993	-0.0981	0.7030	-0.0055	0.7953	-0.0701	0.7747
Fearful	0.0657	0.4692	-0.0921	0.5659	-0.1245	0.7277	-0.0798	0.6837
Solitary	-0.0391	0.4794	0.0989	0.2828	0.0463	0.3125	0.1060	0.4432
Unhappy	0.0492	0.7948	0.2346	0.5117	0.2664	0.5016	0.3889	0.4102
Aches	-0.0078	0.5367	-0.0492	0.4103	-0.0360	0.3897	0.1322	0.1758

Note. The table displays the factors loadings obtained from exploratory factor analysis (EFA) by sample. The EFA is based on the decomposition of the polychoric correlation matrix, and uses oblimin rotation. Since they are all behaviours indicating lower skills, we recode all of them in reverse, i.e. 'Certainly applies' = 0, 'Somewhat applies' = 1, 'Does not apply' = 2.

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Multigroup Factor Model

The relationship between the **latent factors** θ_{ic} and the available **measures** X_{ijc} is characterised by item- and group-specific intercepts v_{jc} and loadings λ_{jc} and is affected by an independent measurement error term u_{ijc} :

$$Z_{ijc}^* = v_{jc} + \lambda_{jc}^\top \theta_{ic} + u_{ijc}$$
(3)

- Dedicated factor structure, where each item loads only on one latent dimension
- Categorical variables $Z_{ijc} \in \{1, 2, ..., L\}$: $Prob\{X_{ijc} = I\} = Pr\{\tau_{l-1} \leq Z_{ijc}^* \leq \tau_l\}$, where $\tau_0 = -\infty$;

$$\theta_{ic} \sim \mathcal{N}(\kappa_c, \sigma_{\theta_c}^2) \quad \text{and} \quad u_{ijc} \sim \mathcal{N}(0, \sigma_c^2)$$
(4)

• Normalisation assumption needed to deal with factor indeterminacy by setting the mean κ_c and the variance $\sigma_{\theta_c}^2$ of the factor equal to 0 and 1. In addition, the intercepts v_{jc} are equal to zero and the error variance σ_c^2 to 1, while the loadings λ_{jc} and threshold τ_{jc} are free to vary.

Measurement invariance

- Estimate three models with additional restrictions that we can compare with the baseline model.
 - Threshold invariant model: observationally equivalent to the baseline model when each item is a categorical variable with three categories (Wu et al. 2016)
 - **2** Loading- and threshold-invariant model: impose that the factor loadings λ_{ic} and the threshold on the parameters must be the same between parents and children
 - **Obsolution** Loading-, threshold-, and intercept-invariant model: impose that the factor loadings λ_{jc} , the intercepts v_{jc} and the threshold be the same between parents and children.

Model	Number of parameters	χ^2	RMSEA	CFI	TLI
Baseline model/ Threshold Invariance	136	1876.094	0.060	0.959	0.948
Threshold and loading invariance	108	2803.019	0.069	0.938	0.932
Threshold, loading, and intercept invariance	81	6457.661	0.100	0.851	0.856

Note. RMSEA stands for the root mean squared error of approximation, CFI for the comparative fit index, and TLI for the Tucker-Lewis index.

Transition matrices **Back**

			(-								
-		Parent quintile									
		1 2 3 4 5									
	1	33.5	15.9	19.3	14.9	12.5					
	2	21.3	21.7	21.7	17.8	19.9					
Child quintile	3	18.3	21.3	22.2	18.3	19					
	4	12.7	21.3	13.5	24	26.9					
	5	14.2	19.8	23.2	25	21.8					

Child's EXT - Parent's EXT (during childhood)

Spectral gap mobility index: 0.800 (0.038)

		Parent quintile						
		1 2 3 4 5						
Child quintile	1	17.2	21.4	18.8	20.3	17.5		
	2	24.2	21.4	15.5	24.6	17.1		
	3	18.7	19.4	20.3	17.4	23		
	4	22.2	19.4	23.2	18.8	15.7		
	5	17.7	18.4	22.2	18.8	26.7		

Spectral gap mobility index: 0.898 (0.031)

Child's INT - Parent's EXT (during childhood)								
	Parent quintile							
	1 2 3 4 5							
Child quintile	1	25.4	13.5	18.8	15.4	22.2		
	2	26.9	21.7	21.3	17.8	13.9		
	3	18.8	19.8	17.4	22.6	21.3		
	4	15.2	21.3	20.8	23.1	21.8		
	5	13.7	23.7	21.7	21.2	20.8		

Spectral gap mobility index: 0.913 (0.025)

Note. All standard errors of the spectral gap mobility index in parentheses are obtained using 200 bootstrap repetition, taking into account the factor estimation stage that precedes the estimation of the transition matrix 15/15 and its respective eigenvalues.

Transition matrices **Back**

			(
		Parent quintile									
		1 2 3 4									
	1	22.7	20.4	18.8	16.9	16.6					
Child quintile	2	21.2	25.7	17.4	19.8	17.1					
	3	22.2	18.4	24.2	18.8	16.6					
	4	18.7	18.4	20.3	21.7	23					
	5	15.2	17	19.3	22.7	26.7					

Child's INT - Parent's INT (during childhood)

Spectral gap mobility index: 0.885 (0.034)

			(-							
		Parent quintile								
		1 2 3 4 5								
	1	26.3	22.8	17.3	20.3	9.3				
	2	23.2	19.9	21.6	19.3	18.5				
Child quintile	3	19.7	24.3	14.9	21.3	19				
	4	15.7	17	23.1	15.5	27.3				
	5	15.2	16	23.1	23.7	25.9				

Child's EXT - Parent's COG (during childhood)

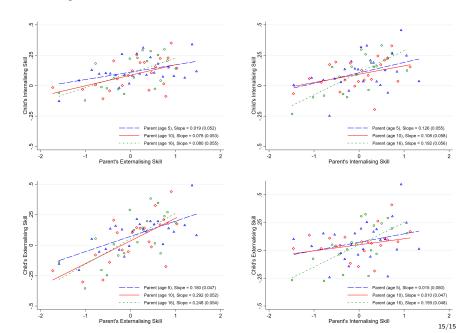
Spectral gap mobility index: 0.844 (0.035)

Child's INT - Parent's COG (during childhood)									
	Parent quintile								
	1 2 3 4 5								
Child quintile	1	25.8	20.4	17.8	18.4	13.4			
	2	25.8	22.3	20.2	20.3	13			
	3	16.2	22.8	19.7	20.3	20.8			
	4	19.2	15	18.8	23.2	25.9			
	5	13.1	19.4	23.6	17.9	26.9			

Spectral gap mobility index: 0.862 (0.038)

Note. All standard errors of the spectral gap mobility index in parentheses are obtained using 200 bootstrap repetition, taking into account the factor estimation stage that precedes the estimation of the transition matrix and its respective eigenvalues.

Mobility without Controls **Lack**



Mobility estimates - age-10 questionnaire administered to teachers of parents **back**

Dependent variable:	Internali	sing (INT) Skills	Externalis	sing (EXT) Skills
	(1)	(2)	(3)	(4)	(5)	(6)
Parent's INT (during childhood)	0.213***	k	0.231***	* 0.127***		0.055
	(0.051)		(0.059)	(0.046)		(0.051)
Parent's EXT (during childhood)	. ,	0.038	-0.044	. ,	0.233***	0.213***
,		(0.048)	(0.060)		(0.046)	(0.055)
Parent's COG (during childhood)	0.114**	0.135***	* 0.124**	0.189***	0.143***	0.140***
	(0.053)	(0.049)	(0.059)	(0.041)	(0.046)	(0.052)
Observations	1144	1144	1144	1144	1144	1144
R^2	0.115	0.079	0.118	0.128	0.157	0.159
Region of birth FE (BCS70 5y)	Yes	Yes	Yes	Yes	Yes	Yes
Child's age FE	Yes	Yes	Yes	Yes	Yes	Yes
Other controls	Yes	Yes	Yes	Yes	Yes	Yes

Note. The measurement system and the intergenerational mobility equation are estimated jointly. All standard errors in parentheses are obtained using 200 bootstrap repetitions (*** p < 0.01, ** p < 0.05, * p < 0.1).